

Name: _____

St George Girls High School

Trial Higher School Certificate Examination

2014



Mathematics

Extension 1

General Instructions

- Reading time – 5 minutes
- Working time – 2 hours
- Write using blue or black pen.
- Write your student number on each booklet.
- Board-approved calculators may be used.
- A table of standard integrals is provided at the back of this paper.
- The mark allocated for each question is listed at the side of the question.
- Marks may be deducted for careless or poorly presented work.

Total Marks – 70

Section I – Pages 2 – 5

10 marks

- Attempt Questions 1 – 10.
- Allow about 15 minutes for this section.
- Answer on the sheet provided.

Section II – Pages 6 – 9

60 marks

- Attempt Questions 11 – 14.
- Allow about 1 hour 45 minutes for this section.
- Begin each question in a new booklet.
- Show all necessary working in Questions 11 – 14.

Students are advised that this is a Trial Examination only and does not necessarily reflect the content or format of the Higher School Certificate Examination.

Section I

10 marks

Marks

Attempt Questions 1 – 10

Allow about 15 minutes for this section

Use the multiple-choice answer sheet for Questions 1–10.

1. If $p(x) = (x + 2)(x + k)$ and if the remainder is 12 when $p(x)$ is divided by $x - 1$, then $k =$

- (A) 2
- (B) 3
- (C) 6
- (D) 11

2. In the diagram drawn below $PB = 12$ cm and $BA = 20$ cm.

P divides AB externally in the ratio

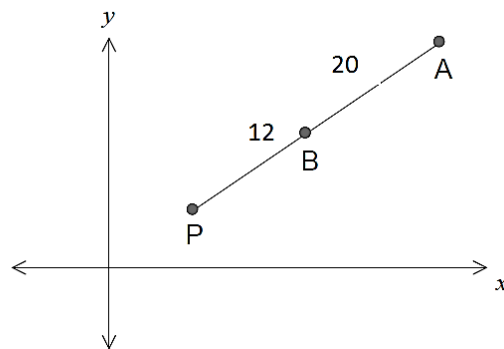


Diagram not to scale

- (A) 3 : 5
- (B) 3 : 8
- (C) 5 : 3
- (D) 8 : 3

Section I (cont'd)

3. If the function f is defined by $f(x) = x^5 - 1$, then f^{-1} , the inverse function of f , is defined by $f^{-1}(x) =$
- (A) $\frac{1}{\sqrt[5]{x+1}}$
- (B) $\frac{1}{\sqrt{x+1}}$
- (C) $\sqrt[5]{x+1}$
- (D) $\sqrt[5]{x} - 1$
4. The coefficient of x^2 in the expansion of $(2x - 3)^5$ is equal to:
- (A) -1080
- (B) -540
- (C) -10
- (D) 1080
5. Which of the following is always true of the perpendicular bisectors of non-parallel chords in the same circle?
- (A) The perpendicular bisectors never intersect
- (B) The perpendicular bisectors are always parallel
- (C) The perpendicular bisectors are always perpendicular to each other
- (D) The perpendicular bisectors always intersect at the centre of the circle
6. What is the domain and range of $y = 3 \sin^{-1}(2x)$?
- (A) Domain : $-\frac{1}{2} \leq x \leq \frac{1}{2}$. Range $-\frac{1}{3} \leq y \leq \frac{1}{3}$
- (B) Domain : $-\frac{1}{2} \leq x \leq \frac{1}{2}$. Range $-\frac{3\pi}{2} \leq y \leq \frac{3\pi}{2}$
- (C) Domain : $-2 \leq x \leq 2$. Range $-\frac{1}{3} \leq y \leq \frac{1}{3}$
- (D) Domain : $-2 \leq x \leq 2$. Range $-\frac{3\pi}{2} \leq y \leq \frac{3\pi}{2}$

Section I (cont'd)

7. If $x = t^3 - t$ and $y = \sqrt{3t + 1}$, then $\frac{dy}{dx}$ at $t = 1$ is:

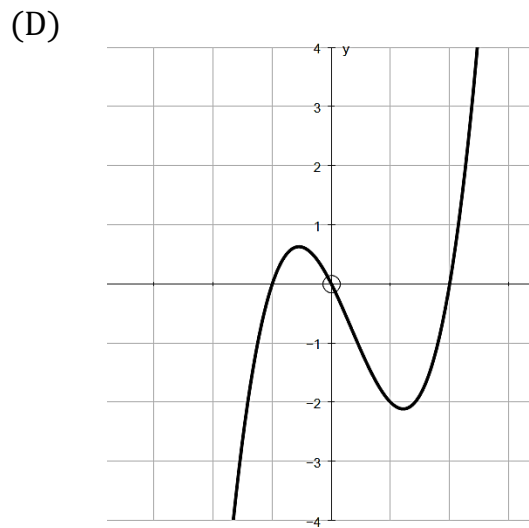
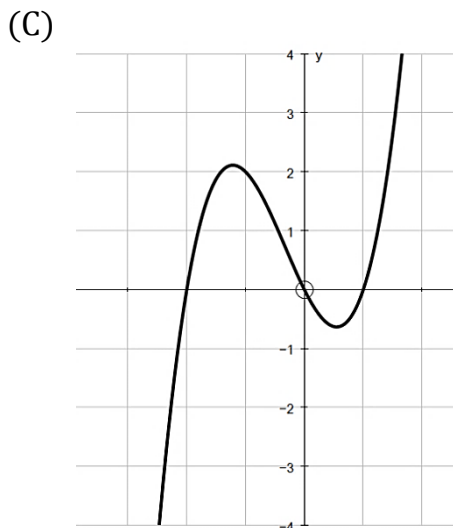
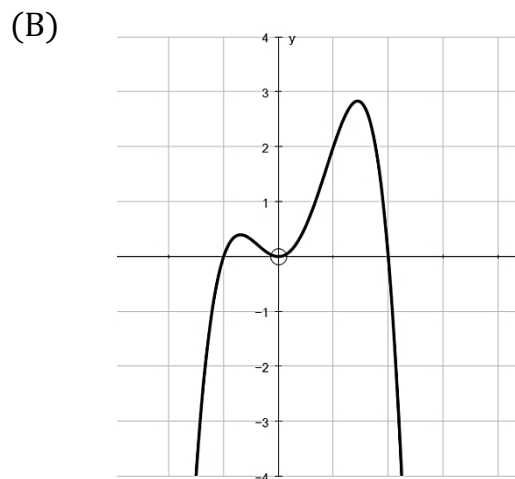
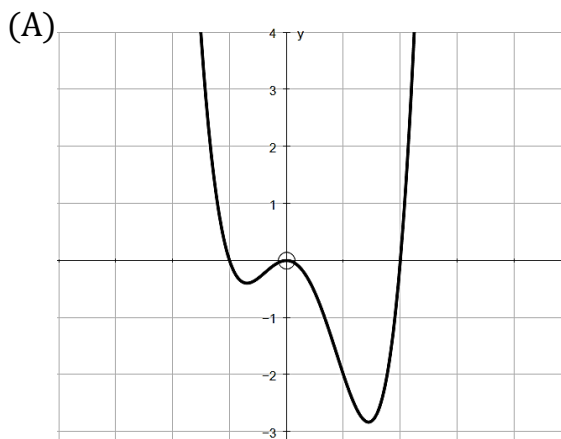
(A) $\frac{1}{8}$

(B) $\frac{3}{8}$

(C) $\frac{3}{4}$

(D) $\frac{8}{3}$

8. Which graph best represents $y = x^4 - x^3 - 2x^2$?



Section I (cont'd)

9. If $y = \sin^{-1}\left(\frac{5}{x}\right)$, $x > 5$, then $\frac{dy}{dx}$ is equal to

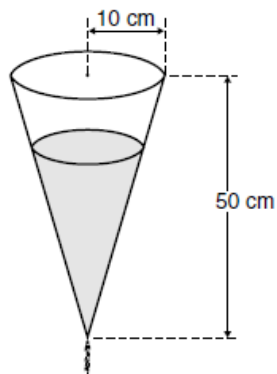
(A) $\frac{-5}{\sqrt{x^2-25}}$

(B) $\frac{x}{\sqrt{x^2-25}}$

(C) $\frac{-5}{x\sqrt{x^2-5}}$

(D) $\frac{-5}{x\sqrt{x^2-25}}$

10.



Water is draining from a cone-shaped funnel at the constant rate of $600 \text{ cm}^3/\text{min}$.

The cone has height 50 cm and base radius 10 cm.

Let h cm be the depth of water in the funnel at time t min.

The rate of **decrease** of h , in cm/min, is given by

(A) 12

(B) $\frac{100\pi}{3}$

(C) $\frac{15000}{\pi h^2}$

(D) $24\pi h^2$

End of Section I

Section II

60 marks

Attempt Questions 11 – 14

Allow about 1 hours 45 minutes for this section

Answer each question in a SEPARATE writing booklet. Extra writing booklets are available.

In Questions 11 – 14, your responses should include relevant mathematical reasoning and/or calculations.

Question 11 (15 marks) Use a SEPARATE writing booklet	Marks
a) The polynomial $4x^3 - 2x^2 + 3x - 5$ has roots α , β and γ . Find $\alpha\beta + \alpha\gamma + \beta\gamma$.	1
b) Find the remainder when $P(x) = 3x^2 - 2x + 1$ is divided by $x - 3$.	2
c) The graphs of $y = 8 - x^3$ and $x - 2y + 13 = 0$ intersect at the point $(1, 7)$. Find the size of the acute angle between the tangent to the curve and the line at the point of intersection. (answer to the nearest minute)	3
d) Find the exact value of $\cos[\sin^{-1}(-\frac{1}{\sqrt{2}})]$.	1
e) Find $\lim_{x \rightarrow 0} \frac{\sin 3x}{2x}$.	1
f) Find $\int \cos^2 2x \, dx$.	2
g) Differentiate $\cos^{-1}(6x^2)$.	2
h) Solve $\frac{4}{6-x} \leq 1$.	3

Question 12 (15 marks) Use a SEPARATE writing booklet **Marks**

a) Use the substitution $u = 5 - x^2$ to evaluate 3

$$\int_0^2 \frac{x}{(5 - x^2)^3} dx .$$

b) What is the coefficient of x^3 in the expansion of $(4x - \frac{2}{x})^5$? 3

c) Prove the identity $\frac{\cos x - \cos 2x}{\sin 2x + \sin x} = \operatorname{cosec} x - \cot x$. 3

d) Use mathematical induction to prove that $9^n - 3$ is divisible by 6 for all positive integers n . 3

e) For the polynomial $P(x) = x^3 + 5x^2 + 17x - 10$

(i) Show it has a root that lies between 0 and 2 . 1

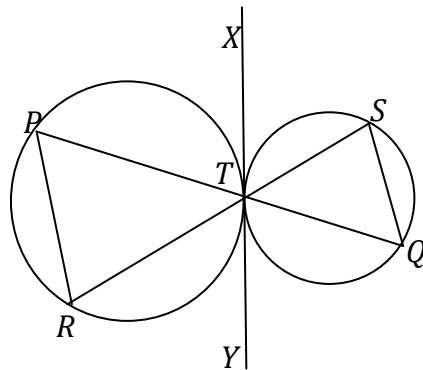
(ii) Use one application of Newton's method with an initial estimate of 1, to find a better approximation the root. 2

Question 13 (15 marks) Use a SEPARATE writing booklet

Marks

a)

3

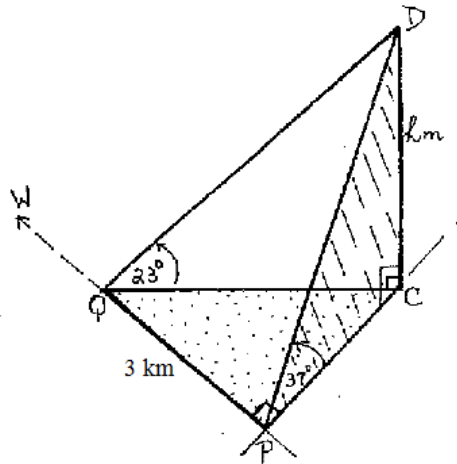


Two circles touch externally at T . XY is the common tangent.

PTQ and RTS are straight lines. Prove that PR is parallel to SQ .

- b) The angular elevation of a hill at a place P due south of it is 37° and at a place Q due west of P the elevation is 23° as shown in the diagram below. If the distance from P to Q is 3 km, find the height of the hill to the nearest 10 metres.

4



- c) A particle is projected from a point O on a horizontal plane with an initial velocity of 60 metres/second at an angle of 30° to the horizontal. Assume acceleration due to gravity is 10 m/s^2 .

(i) Write down the equation (in exact form) for velocity and displacement of the particle in both the horizontal and vertical directions.

4

(ii) Find the range of the particle.

2

(iii) At the same time a second particle is projected in the opposite direction with an initial velocity of 50 metres/second from a point on the same horizontal level as O . Find the angle of projection of the second particle if the particles collide (to the nearest degree).

2

Question 14 (15 marks) Use a SEPARATE writing booklet **Marks**

- a) $P(2p, p^2)$ and $Q(2q, q^2)$ are two points on the parabola $x^2 = 4y$.
- (i) Find the coordinates of M , the mid point of PQ . 1
- (ii) Show $pq = -4$ if PQ subtends a right angle at the origin. 2
- (iii) Using your answers to parts (i) and (ii), find the equation of the locus of M as P and Q move on the parabola if $\angle POQ = 90^\circ$. 2

- b) A particle moves in such a way that its displacement x cm from the origin O after time t seconds is given by:

$$x = \sqrt{3} \cos 3t - \sin 3t .$$

- (i) Show that the particle moves in simple harmonic motion. 2
- (ii) Evaluate the period of the motion. 2
- (iii) Find the time when the particle first passes through the origin. 3

- c) By equating the coefficient of x^n on both sides of the identity 3

$$(1 + x)^n(1 + x)^n = (1 + x)^{2n} ,$$

Show that
$$\binom{n}{0}^2 + \binom{n}{1}^2 + \binom{n}{2}^2 + \dots + \binom{n}{n-1}^2 + \binom{n}{n}^2 = \frac{(2n)!}{(n!)^2} .$$

MC

1) $P(1) = 12 \quad 12 = 3(1+k)$
 $\therefore k = 3$

B

2) $AP : PB = 32 : 12$
 $= 8 : 3$

D

3) $y = x^5 - 1$

$f^{-1}: x = y^5 - 1 \quad y = \sqrt[5]{x+1}$
 $x+1 = y^5$

C

4) $(2x-3)^5 = \sum_{i=0}^5 {}^5C_i (2x)^{5-i} (-3)^i$

$x^2: 5-i = 2 \quad \therefore i = 3$

${}^5C_3 2^2 (-3)^3 = 10 \times 4 \times -27$
 $= -1080$

A

5)

D

6) $y = 3 \sin^{-1}(2x)$

$\frac{y}{3} = \sin^{-1}(2x)$

B

$f^{-1} \quad y = \sin^{-1} x$

A: $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$

B: $-\frac{\pi}{2} \leq \frac{y}{3} \leq \frac{\pi}{2}$

$-\frac{3\pi}{2} \leq y \leq \frac{3\pi}{2}$

D: $-1 \leq x \leq 1$

$-1 \leq 2x \leq 1$

$-\frac{1}{2} \leq x \leq \frac{1}{2}$

7) $x = t^3 - t$

$\frac{dx}{dt} = 3t^2 - 1$

$y = (3t+1)^{1/2}$
 $\frac{dy}{dt} = \frac{3}{2} (3t+1)^{-1/2}$

B

$\frac{dy}{dx} = \frac{3}{2} (3t+1)^{-1/2}$

$\times \frac{1}{3t^2-1}$

at $t=1$

$\frac{dy}{dx} = \frac{3}{2} \times \frac{1}{2} \times \frac{1}{2}$
 $= \frac{3}{8}$

$$8) \quad \begin{array}{l} x \rightarrow \infty \quad y \rightarrow \infty \\ x \rightarrow -\infty \quad y \rightarrow \infty \end{array}$$

$$y = x^2(x^2 - x - 2)$$

$$= x^2(x-2)(x+1) \quad \therefore A$$

$$9) \quad y = \sin^{-1}\left(\frac{5}{x}\right)$$

$$\text{Let } \frac{5}{x} = m$$

$$y = \sin^{-1} m$$

$$-\frac{5}{x^2} = \frac{dm}{dx}$$

$$\frac{dy}{dm} = \frac{1}{\sqrt{1-m^2}}$$

$$\frac{dy}{dx} = \frac{dy}{dm} \times \frac{dm}{dx}$$

$$= \frac{1}{\sqrt{1-\left(\frac{5}{x}\right)^2}} \times -\frac{5}{x^2}$$

$$= \frac{-5}{x\sqrt{x^2-25}}$$

D

$$10) \quad \frac{dV}{dt} = 600$$

$$V = \frac{1}{3}\pi r^2 h$$

$$\text{where } 5r = h$$

$$r = \frac{h}{5}$$

$$= \frac{1}{3}\pi \left(\frac{h}{5}\right)^2 h$$

$$= \frac{\pi h^3}{75}$$

$$\frac{dV}{dh} = \frac{\pi h^2}{25}$$

$$\frac{dh}{dt} = \frac{dh}{dV} \cdot \frac{dV}{dt}$$

$$= \frac{25}{\pi h^2} \times 600$$

$$= \frac{15000}{\pi h^2}$$

C

$$\begin{aligned}
 f) \int \cos^2 2x \, dx &= \frac{1}{2} \int (\cos 4x + 1) \, dx \\
 &= \frac{1}{2} \left[\frac{1}{4} \sin 4x + x \right] + C \\
 &= \frac{1}{8} \sin 4x + \frac{1}{2} x + C
 \end{aligned}$$

$$g) y = \cos^{-1}(6x^2)$$

$$\text{let } m = 6x^2$$

$$\frac{dm}{dx} = 12x$$

$$y = \cos^{-1} m$$

$$\frac{dy}{dm} = -\frac{1}{\sqrt{1-m^2}}$$

$$\frac{dy}{dx} = \frac{dy}{dm} \times \frac{dm}{dx}$$

$$= -\frac{1}{\sqrt{1-(6x^2)^2}} \times 12x$$

$$= -\frac{12x}{\sqrt{1-36x^4}}$$

$$h) \frac{4}{6-x} \leq 1 \quad x \neq 6$$

$$4(6-x) \leq 1 \cdot (6-x)^2$$

$$0 \leq (6-x)^2 - 4(6-x)$$

$$(6-x)(6-x-4) \geq 0$$

$$(6-x)(2-x) \geq 0$$



$$x \leq 2 \quad \text{or} \quad x > 6 \quad \text{BUT } x \neq 6$$

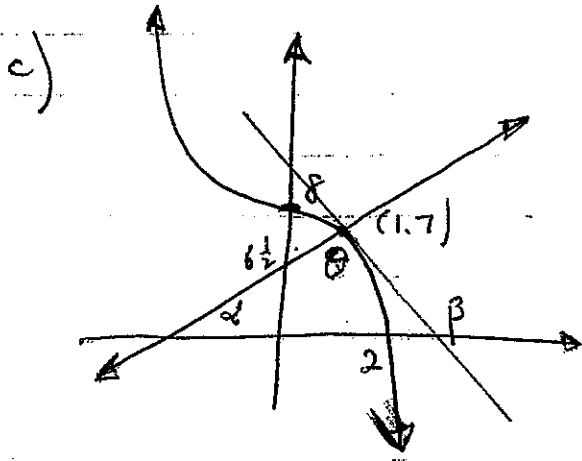
$$\therefore x \leq 2 \quad \text{or} \quad x > 6$$

Q 11

$$\begin{aligned} \text{a) } \alpha\beta + \alpha\gamma + \beta\gamma &= \frac{c}{a} \\ &= \frac{3}{7} \end{aligned}$$

$$\begin{aligned} \text{b) } P(3) &= 27 - 6 + 1 \\ &= 22 \end{aligned}$$

Remainder is 22



$$\theta = \beta - \alpha$$

$$y = 8 - x^3$$

$$y' = -3x^2$$

$$\text{at } x=1 \quad m = -3 \quad \tan \beta = -3$$

$$x - 2y + 13 = 0$$

$$m = \frac{1}{2}$$

$$\tan \alpha = \frac{1}{2}$$

or

$$\begin{aligned} \tan \theta &= \frac{-3 - \frac{1}{2}}{1 + (-3)(\frac{1}{2})} \\ &= \frac{-\frac{7}{2}}{-\frac{1}{2}} \end{aligned}$$

$$= -7$$

$$\theta = 81^\circ 52'$$

$$\begin{aligned} \theta &= \tan^{-1}(-3) - \tan^{-1}(\frac{1}{2}) \\ &= 81^\circ 52' \end{aligned}$$

$$\begin{aligned} \text{d) } \cos(\sin^{-1}(-\frac{1}{\sqrt{2}})) &= \cos(-\frac{\pi}{4}) \\ &= \frac{1}{\sqrt{2}} \end{aligned}$$

$$\begin{aligned} \text{e) } \lim_{x \rightarrow 0} \frac{\sin 3x}{2x} &= \lim_{x \rightarrow 0} \frac{\sin 3x}{3x \times \frac{2}{3}} \\ &= \frac{3}{2} \lim_{x \rightarrow 0} \frac{\sin 3x}{3x} = \frac{3}{2} \end{aligned}$$

Q12

a) $u = 5 - x^2$

$x = 2 \quad u = 1$

$du = -2x dx$

$x = 0 \quad u = 5$

$$\begin{aligned} \int_0^2 \frac{x}{(5-x^2)^3} dx &= -\frac{1}{2} \int_0^2 \frac{-2x}{(5-x^2)^3} dx \\ &= -\frac{1}{2} \int_5^1 \frac{du}{u^3} \\ &= \frac{1}{2} \int_1^5 u^{-3} du \\ &= \frac{1}{2} \left[-\frac{1}{2} u^{-2} \right]_1^5 \\ &= -\frac{1}{4} \left[5^{-2} - 1^{-2} \right] \\ &= -\frac{1}{4} \left[\frac{1}{25} - 1 \right] \\ &= -\frac{1}{4} \times -\frac{24}{25} \\ &= \frac{6}{25} \end{aligned}$$

b) $\left(4x - \frac{2}{x}\right)^5 = \sum_{i=0}^5 {}^5C_i (4x)^{5-i} \left(-\frac{2}{x}\right)^i$

$x^3 : \quad x^{5-i} \cdot (x^{-1})^i = x^3$

$5 - i - i = 3$

$i = 1$

Co-efficient ${}^5C_1 4^4 \cdot (-2)^1 = 5 \times 256 \times -2 = -2560$

$$\begin{aligned}
 \text{c) } \frac{\cos x - \cos 2x}{\sin 2x + \sin x} &= \frac{\cos x - [2\cos^2 x - 1]}{2\sin x \cos x + \sin x} \\
 &= \frac{-(2\cos^2 x - \cos x - 1)}{\sin x (2\cos x + 1)} \\
 &= \frac{-(\cancel{2\cos x + 1})(\cos x - 1)}{\sin x (\cancel{2\cos x + 1})} \\
 &= \frac{1 - \cos x}{\sin x} \\
 &= \operatorname{cosec} x - \cot x \\
 &\quad (\text{as required})
 \end{aligned}$$

$$\begin{aligned}
 \text{d) Step 1: For } n=1 \quad 9^1 - 3 &= 9 - 3 \\
 &= 6 \\
 \therefore \text{true for } n=1
 \end{aligned}$$

Step 2: Assume true for $n=k$

$$9^k - 3 = 6m \quad (\text{for some integer } m)$$

Now for $n=k+1$

$$\begin{aligned}
 9^{k+1} - 3 &= 9 \cdot 9^k - 3 \\
 &= 9(6m + 3) - 3 \\
 &= 54m + 27 - 3 \\
 &= 6(9m + 4)
 \end{aligned}$$

As m is an integer $9m+4$ is integral
Step 3 \therefore true for $n=k+1$ when true for

$n=k$ and as true for $n=1$ then true for $n=2$ and all integers n .

$$e)(i) P(x) = x^3 + 5x^2 + 17x - 10$$

$$P(0) = -10$$

$$P(2) = 8 + 20 + 34 - 10 = 52$$

\therefore root between $x=0$ and $x=2$

So we use $x=1$ as an estimate

$$(ii) x_1 = 1 - \frac{P(1)}{P'(1)}$$

$$= 1 - \frac{13}{30}$$

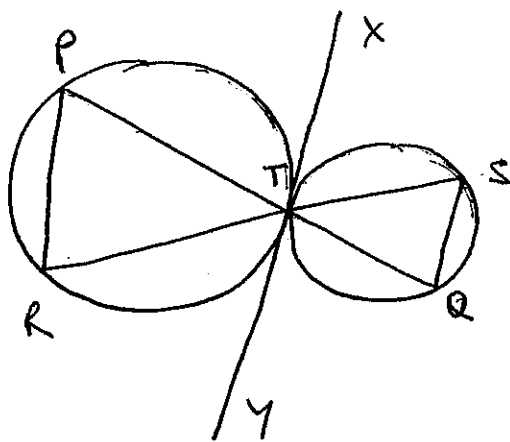
$$= \frac{17}{30}$$

$$P'(x) = 3x^2 + 10x + 17$$

$$P'(1) = 30$$

Q 13

a)



$$\angle XTP = \angle YTS$$

(vertically opposite)

$$\angle XTP = \angle PRT$$

(angle in the alternate segment)

$$\angle YTS = \angle QST$$

(angle in alternate segment)

$$\text{So } \angle PRT = \angle QST$$

$$\therefore PR \parallel SQ \text{ (alternate angles equal)}$$

$$b) \text{ In } \triangle PCD$$

$$\frac{h}{PC} = \tan 37^\circ$$

$$PC = \frac{h}{\tan 37^\circ}$$

$$\triangle QCD$$

$$\frac{h}{QC} = \tan 23^\circ$$

$$QC = \frac{h}{\tan 23^\circ}$$

$$QC^2 = QP^2 + PC^2$$

$$\frac{h^2}{\tan^2 23^\circ} = 3^2 + \frac{h^2}{\tan^2 37^\circ}$$

Q 14

a) $P(2p, p^2)$ $Q(2q, q^2)$ $a=1$
 $x^2=4y$

(i) $M\left(\frac{2p+2q}{2}, \frac{p^2+q^2}{2}\right)$ where M is midpoint of PQ
 $M\left(p+q, \frac{p^2+q^2}{2}\right)$

(ii) $M_{OP} = \frac{p^2}{2p}$ $M_{OQ} = \frac{q^2}{2q}$ M is gradient
 $= \frac{p}{2}$ $= \frac{q}{2}$

When $\angle POQ = 90^\circ$ $\frac{p}{2} \times \frac{q}{2} = -1$
 $pq = -4$

(iii) $x = p+q$ $x^2 = p^2 + 2pq + q^2$
 $y = \frac{p^2+q^2}{2}$ $= p^2 + q^2 - 8$
 $y = \frac{x^2+8}{2}$ $\therefore x^2+8 = p^2+q^2$
 $y = \frac{1}{2}x^2 + 4$ $x^2 = 2(y-4)$

\therefore locus is a parabola $V(0, 4)$
focal length $\frac{1}{2}$

b) $x = \sqrt{3} \cos 3t - \sin 3t$

(i) $\dot{x} = -3\sqrt{3} \sin 3t - 3 \cos 3t$

$\ddot{x} = -9\sqrt{3} \cos 3t + 9 \sin 3t$
 $= -9(\sqrt{3} \cos 3t - \sin 3t)$

$$h^2 \left[\frac{1}{\tan^2 23^\circ} - \frac{1}{\tan^2 37^\circ} \right] = 9$$

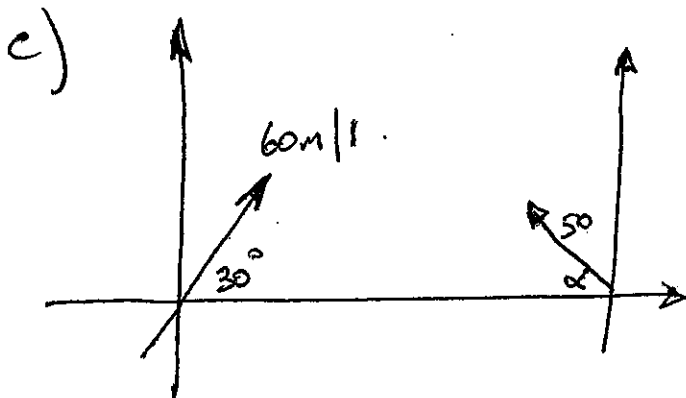
$$h^2 \left[\frac{\tan^2 37^\circ - \tan^2 23^\circ}{\tan^2 23^\circ \tan^2 37^\circ} \right] = 9$$

$$h^2 = 9 \left[\frac{\tan^2 23^\circ \tan^2 37^\circ}{\tan^2 37^\circ - \tan^2 23^\circ} \right]$$

$$= 2.3753017$$

$$h = 1.5412014$$

\therefore Hill is 1540 m high (to nearest 10 m)



$$(i) \quad \ddot{x} = 0 \quad \ddot{y} = -10$$

$$\dot{x} = c \quad \dot{y} = -10t + c$$

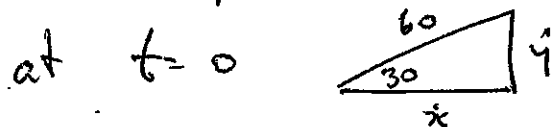
$$\boxed{x = 30\sqrt{3}} \quad \boxed{y = -10t + 30}$$

$$x = 30\sqrt{3}t + c \quad y = -5t^2 + 30t + c$$

$$t = 0 \quad x = 0 \quad y = 0$$

$$\boxed{x = 30\sqrt{3}t}$$

$$\boxed{y = -5t^2 + 30t}$$



$$\frac{\dot{x}}{60} = \cos 30^\circ \quad \frac{\dot{y}}{60} = \sin 30^\circ$$

$$\dot{x} = 60 \times \frac{\sqrt{3}}{2} \quad \dot{y} = 60 \times \frac{1}{2}$$

$$= 30\sqrt{3} \quad = 30$$

$$(ii) \quad y = 0 \quad 5t^2 - 30t = 0$$

$$5t(t - 6) = 0$$

$$\therefore t = 0 \text{ or } 6$$

$$t = 6 \quad x = 180\sqrt{3}$$

\therefore RANGE is $180\sqrt{3}$ m

$$(iii) \quad \dot{y} = -10t + c$$

$$\dot{y} = -10t + 50 \sin \alpha$$

$$y = -5t^2 + 50t \sin \alpha$$

$$\text{So } 30t = 50t \sin \alpha$$

$$\sin \alpha = \frac{3}{5}$$

$$\alpha = 37^\circ \text{ (nearest degree)}$$

$$\ddot{x} = -9x$$

1. Motion is SHM with $n=3$ centre of motion $x=0$.

$$(ii) T = \frac{2\pi}{n}$$

$$= \frac{2\pi}{3}$$

$$(iii) \sqrt{3} \cos 3t - \sin 3t = 0$$

$$\frac{\sqrt{3} \cos 3t}{\sqrt{3}} = \frac{\sin 3t}{\sqrt{3}}$$

$$\cos 3t = \frac{\sin 3t}{\sqrt{3}}$$

$$\tan 3t = \sqrt{3}$$

$$3t = \frac{\pi}{3}, \dots$$

$$t = \frac{\pi}{9}$$

First passes through origin after $\frac{\pi}{9}$ sec.

$$e) (1+x)^n (1+x)^n = (1+x)^{2n}$$

$$LHS = (1+x)^n (1+x)^n$$

$$= \left({}^n C_0 + {}^n C_1 x + {}^n C_2 x^2 + \dots + {}^n C_n x^n \right) \left({}^n C_0 + {}^n C_1 x + \dots + {}^n C_n x^n \right)$$

$$\text{coeff of } x^n: {}^n C_0 {}^n C_n + {}^n C_1 {}^n C_{n-1} + {}^n C_2 {}^n C_{n-2} + \dots + {}^n C_{n-1} {}^n C_1 + {}^n C_n {}^n C_0$$

$$\text{Now as } {}^n C_{n-r} = {}^n C_r$$

$$= \left({}^n C_0 \right)^2 + \left({}^n C_1 \right)^2 + \dots + \left({}^n C_{n-1} \right)^2 + \left({}^n C_n \right)^2$$

$$\text{coeff of } x^n \text{ in RHS } \quad {}^{2n} C_n = \frac{(2n)!}{n! n!}$$

$$\therefore \binom{n}{0}^2 + \binom{n}{1}^2 + \dots + \binom{n}{n}^2 = \frac{(2n)!}{n! n!}$$