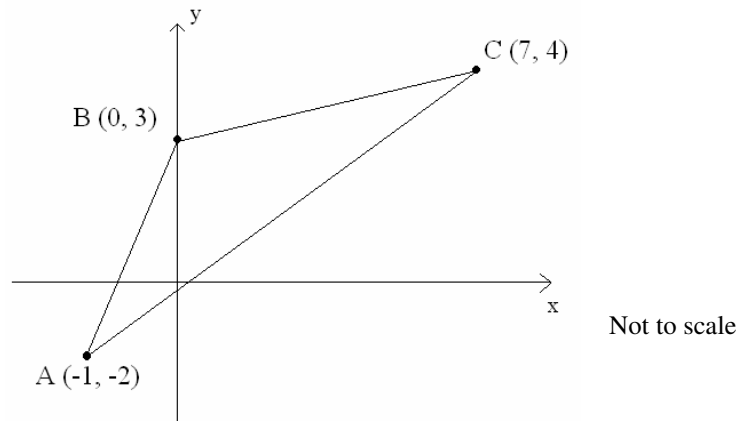


<b>QUESTION 1</b> [12 marks]	<b>Marks</b>
(a.) Evaluate, correct to three significant figures $\sqrt{\frac{(2.044)^3}{35.5 - 1.2^2}}$	2
(b.) Solve for $x$ : $x^3 = 6x^2$	2
(c.) Differentiate with respect to $x$ $y = e^{x^2 - 4x}$	2
(d.) Solve the pair of simultaneous equations $2x + 3y = -1$ $3x - y = 15$	2
(e.) Find a primitive of $\sin \frac{x}{2}$	1
(f.) Solve $ 7 - 3x  \geq 2$ and graph your solution on the number line	3

**QUESTION 2** [12 marks]

(a.) If $\cos \theta = \frac{2}{5}$ and $\tan \theta < 0$ , find the exact value of $\sin \theta$	2
(b.) Differentiate	
i.) $x^2 \ln x$	2
ii.) $\frac{\sqrt{x}}{3x - 2}$	2
(c.) Find $\int \frac{x^2}{x^3 + 5} dx$	2
(d.) Evaluate $\int_0^{\ln 3} e^{2x} dx$	2
(e.) Solve $e^{\log_e x^3} = 27$	2

**QUESTION 3** [12 marks]**Marks**

The diagram shows  $\triangle ABC$  with vertices  $A(-1, -2)$ ,  $B(0, 3)$  and  $C(7, 4)$ . Copy the diagram onto your answer sheet.

- |             |  |          |
|-------------|--|----------|
| <b>(a.)</b> | E is the midpoint of AC. Find the coordinates of E   | <b>1</b> |
| <b>(b.)</b> | Find the gradient of AC  | <b>1</b> |
| <b>(c.)</b> | A line $l$ is drawn through B, perpendicular to AC.<br>Show that the equation of line $l$ is $4x + 3y - 9 = 0$ | <b>2</b> |
| <b>(d.)</b> | What is the angle that $l$ makes with the positive $x$ axis?   | <b>1</b> |
| <b>(e.)</b> | Find the perpendicular distance of B from AC   | <b>2</b> |
| <b>(f.)</b> | Find the area of $\triangle ABC$   | <b>2</b> |
| <b>(g.)</b> | AC is the diameter of a circle   |          |
|             | i.) Calculate the radius of the circle   | <b>1</b> |
|             | ii.) Hence find the equation of the circle   | <b>2</b> |

**QUESTION 4** [12 marks]

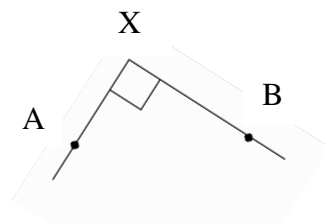
- |             |  |          |
|-------------|--|----------|
| <b>(a.)</b> | Given the parabola $y = 2x^2 - 8x + 1$ , find: |          |
|             | i.) focal length                               | <b>1</b> |
|             | ii.) vertex                                    | <b>1</b> |
|             | iii.) focus                                    | <b>1</b> |
|             | iv.) directrix                                 | <b>1</b> |

**QUESTION 4 (continued)****Marks**

- (b.) The third term and the tenth term of an arithmetic series are 10 and 31 respectively. Find the:
- i.) first term and the common difference 2
  - ii.) sum of the first ten terms of the series 1
- (c.) Using Simpson's Rule with three function values, find an approximate value for the area represented by the definite integral 3
- $$\int_2^3 \cos^2 x \, dx$$
- (d.) One hundred tickets are sold in a raffle. Two different tickets are to be drawn for first and second prizes. Bianca buys 15 tickets. What is the probability that she:
- i.) wins first prize 1
  - ii.) wins at least one prize 1

**QUESTION 5 [12 marks]**

- (a.) Find the equation of the tangent to the curve  $y = \ln(x^2 + 2)$  at the point where  $x = 1$ . Answer in general form 4
- (b.) The gradient of the curve  $y = f(x)$  is given by  $f'(x) = \frac{2x^2 + 1}{x}$ . 3  
Find the equation of the curve if it passes through the point (1, 5)
- (c.)



Two athletes are jogging on separate roads which meet at right angles at town X. Athlete A is 8km from X and is travelling at 5km/h away from X. Athlete B is 10km from X and is travelling at 6km/h and travelling towards X.

- i.) Show that the distance apart,  $P$  km, after  $t$  hours is given by 2  
$$P = \sqrt{61t^2 - 40t + 164}$$
- ii.) Hence find their minimum distance apart. 3

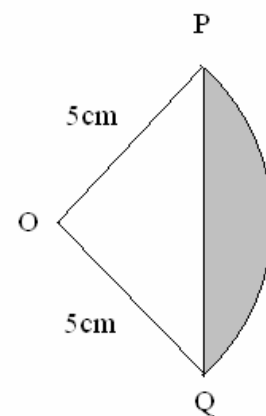
**QUESTION 6** [12 marks]**Marks**

- (a.) Consider the curve  $y = x(x - 3)^3$
- i.) Find the coordinates of any stationary points and determine their nature **4**
- ii.) Find the point(s) of inflexion **2**
- iii.) Sketch the curve, showing clearly all features **1**
- (b.) If  $\alpha, \beta$  are roots of the quadratic equation  $6x^2 - x + 5 = 0$ , find:
- i.)  $\alpha + \beta$  **1**
- ii.)  $\alpha \times \beta$  **1**
- iii.)  $\alpha^2 + \beta^2$  **1**
- (c.) Solve  $\log_{27} 32 = x \log_3 2$  without the aid of a calculator. Show all working **2**

**QUESTION 7** [12 marks]

- (a.) i.) Draw a neat sketch of the function  $y = 1 - 2\sin x$  for  $0 \leq x \leq 2\pi$  **2**
- ii.) Determine the exact values where the graph cuts the  $x$ -axis in the given domain **2**
- iii.) Calculate the area bounded by the curve  $y = 1 - 2\sin x$ , the  $x$ -axis and the lines  $x = 0$  and  $x = \frac{\pi}{2}$  **2**

- (b.) In the diagram PQ is an arc of a circle with centre O and radius 5cm. The chord PQ has length 6cm.



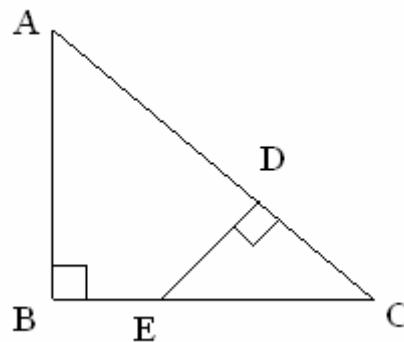
- i.) Find the size of  $\angle POQ$  in radians **2**
- ii.) Calculate the shaded area **2**

**QUESTION 7 (continued)****Marks**

- (c.) Find the values of  $K$  for which the equation  $(2 - K)x^2 - 4(K - 2)x - 5 = 0$ , has two real distinct roots **2**

**QUESTION 8 [12 marks]**

- (a.) A particle, initially at rest at the origin, moves in a straight line with velocity  $V$  m/s so that  $V = 5t(4 - t)$  where  $t$  is the time in seconds. Find:
- i.) the acceleration of the particle after 4 seconds **2**
  - ii.) an expression for the displacement  $x$  metres of the particle in terms of  $t$  **2**
  - iii.) the total distance travelled in the first 6 seconds **2**

**(b.)**

Not to scale

ABC is right angled at B and DE is perpendicular to AC.

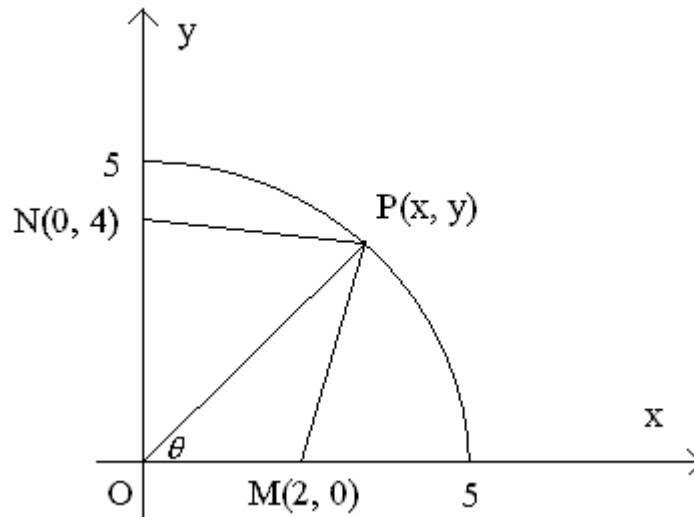
- i.) Prove that  $\triangle ABC$  and  $\triangle CDE$  are similar **2**
- ii.) Prove that  $BC \times CE = AC \times CD$  **2**
- iii.) Prove that  $DE^2 = AD \times DC - BE \times EC$  **2**

**QUESTION 9** [12 marks]**Marks**

- (a.) A bottle of solvent is open and the solvent evaporates in such a way that the amount remaining,  $V$  ml, in the bottle is given by  $V = 2000e^{-0.005t}$ , where  $t$  is time in hours.
- i.) How much solvent is in the bottle initially? **1**
- ii.) How much solvent has evaporated out of the bottle after 30 hours? **1**
- iii.) How long is it before half the initial amount of solvent has evaporated from the bottle? **1**
- iv.) If the solvent continues to evaporate will the bottle ever become empty? Explain. **1**
- (b.) Boxes in a storeroom are stacked in a pile such that there are 25 on the bottom row, 22 on the next, 19 on the next, and so on until 117 boxes are on the pile altogether.
- i.) How many rows of boxes are there? **2**
- ii.) How many boxes are there on the top row? **1**
- (c.) By expressing  $1.2\dot{5}$  as the sum of an infinite geometric series, find the simple equivalent fraction for  $1.2\dot{5}$ . **2**
- (d.) The graph  $y = e^x - 1$  is rotated about the  $x$ -axis from  $x = 1$  to  $x = 3$ . **3**  
Find the volume generated.

**QUESTION 10** [12 marks]

**Marks**



- (a.) The diagram shows a part of the circle  $x^2 + y^2 = 25$ . The point  $P(x, y)$  is on the circle and  $O$  is the origin. Given  $M(2, 0)$  and  $N(0, 4)$  and  $\angle MOP$  is  $\theta$  radians.
- i.) Show that the area  $A$ , of the quadrilateral  $OMPN$  is given by 2  
 $A = 5\sin\theta + 10\cos\theta$
- ii.) Find the value of  $\tan\theta$  for which  $A$  is maximum 3
- iii.) Hence find (in surd form) the coordinates of  $P$  2  
 for which  $A$  is maximum
- (b.) Alice is retiring tomorrow and her Super Fund contains \$450,000. The fund is earning 15% p.a. compound interest, compounded monthly. Alice wishes to withdraw a regular amount of \$6000 per month to cover her expenses.
- i.) Show that after 1 month she will have an amount  $A$  in her account 1  
 where  $A_1 = 450000 \times 1.0125 - 6000$
- ii.) Find an expression for the amount remaining after  $n$  months 1
- iii.) How many years will the money last? 2
- iv.) If she wishes to withdraw \$6000 per month from her account for 1  
 30 years, use your calculator to approximate the required interest rate.

**End of Paper**

Yr. 12 TRIAL 2007 – Answers – TOTAL (120)

Question 1 (12)

(a)  $0.5007 = 0.501$  (3s.f.)

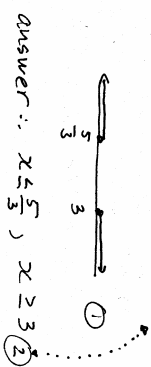
b)  $x^3 = 6x^2$   
 $x^3 - 6x^2 = 0$   
 $x^2(x - 6) = 0$   
 $x = 0$  or  $x = 6$

c)  $y_1 = e^{x^2 - 4x}$   
 $y_2 = (2x - 4) \cdot e^{x^2 - 4x}$

d)  $2x + 3y = -1$   
 $3x - y = 15$   
 $x = 4$  or  $y = -3$

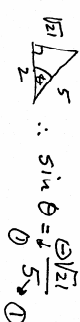
e)  $\int \sin \frac{x}{2} dx = -\frac{1}{\frac{1}{2}} \cos \frac{x}{2} + c$   
 $= -2 \cos \frac{x}{2} + c$

f)  $|7 - 3x| \geq 2$   
 $7 - 3x \geq 2$  or  $7 - 3x \leq -2$   
 $-5 \geq 3x$  or  $9 \leq 3x$   
 $\frac{-5}{3} \geq x$  or  $3 \leq x$



Question 2 (12)

(a)  $\cos \theta = \frac{2}{5}$  or  $\tan \theta < 0$



(b) i)  $\frac{d}{dx} (x^2 \ln x^2) = 2x \cdot \ln x^2 + x^2 \cdot \frac{2x}{x^2}$   
 $= 2x \cdot \ln x^2 + 2x$

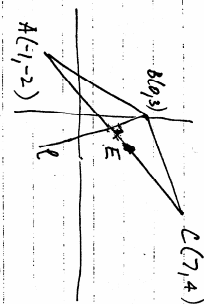
ii)  $\left( \frac{\sqrt{x}}{3x-2} \right)' = \frac{\frac{1}{2}x^{-1/2}(3x-2) - \sqrt{x}(3)}{(3x-2)^2}$

(c)  $\int \frac{x^2}{x^3+5} dx = \frac{1}{3} \ln(x^3+5) + c$

(d)  $\int_0^{1/3} e^{2x} dx = \frac{1}{2} [e^{2x}]_0^{1/3} = \frac{1}{2} (e^{2/3} - 1)$

e)  $e^{\log_e x^3} = 27$   
 $x^3 = 27$   
 $x = 3$

Question 3 (12)



(a)  $E(3, 1)$

(b)  $m_{AC} = \frac{4-2}{7-(-1)} = \frac{2}{8} = \frac{1}{4}$

(c)  $m_l = -\frac{4}{3}$   
 $\therefore l: y - 3 = -\frac{4}{3}(x - 0)$   
 $y = -\frac{4}{3}x + 3$

(d)  $\tan \theta = m_l = -\frac{4}{3}$   
 $\therefore \theta = 126.87^\circ$

e)  $B(0, 3)$   
 line AC:  $y - 4 = \frac{2}{8}(x - 7)$   
 $3x - 4y - 5 = 0$

$d = \frac{|3(0) - 4(3) - 5|}{\sqrt{3^2 + (-4)^2}} = \frac{17}{5}$

f) Area =  $\frac{1}{2} AC \times d = 10$

Area =  $\frac{1}{2} \times 10 \times \frac{17}{5} = 17$

g) i)  $r = \frac{1}{2} AC = 5$   
 ii)  $E(3, 1)$  centre,  $r = 5$   
 $\therefore (x-3)^2 + (y-1)^2 = 5^2$

Question 4 (12)

(a)  $y = 2x^2 = 8x + 1$   
 $(x-m)^2 = 4a(y-n)$   
 $(x-2)^2 = \frac{1}{2}(y+7)$

- i) focal length =  $a = \frac{1}{2}$
- ii) vertex  $(2, -7)$
- iii) focus  $(2, -6\frac{1}{2})$
- iv) directrix  $y = -7\frac{1}{2}$

(b)  $I_3 = a + 2d = -10$   
 $I_7 = a + 9d = -31$

(c)  $d = 3$  or  $a = 4$   
 $\int_0^2 \cos^2 x dx = \frac{x}{2} + \frac{\sin 2x}{4}$   
 $= \frac{2}{2} + \frac{\sin 4}{4} = 1 + \frac{\sin 4}{4}$

$P = \frac{0.5}{3} [0.17318 + 4 \times 0.64183 + 0.9209]$   
 $= 0.62009 \approx 0.62$

(d) i)  $P = \frac{15}{100}$   
 ii)  $P = 1 - P(\text{no prize})$   
 $= 1 - \frac{85}{100} \times \frac{84}{99}$   
 $P = 0.278$  or  $\frac{143}{500}$



Question 5 (12)

(a)  $y = 14(x^2 + 2)$   
 $y' = \frac{2x}{x^2 + 2}$   
 $m = \frac{2}{3}$  (i)  $y = 14x$   
 $\therefore y - 14x = \frac{2}{3}(x - 1)$   
 $0 = 2x - 3y - 2 + 3 \ln 3$   
 or  
 $0 = 2x - 3y - 2 + \ln 27$

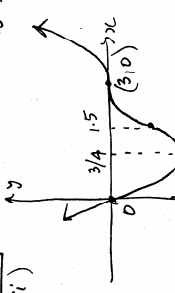
(b)  $f(x) = \frac{2x^2 + 1}{x}$   
 $f(x) = \int \frac{2x^2 + 1}{x} dx$   
 $= \int (2x + \frac{1}{x}) dx$   
 $f(x) = x^2 + \ln|x| + C$   
 $5 = 1 + 0 + C \therefore C = 4$   
 $\therefore f(x) = x^2 + \ln|x| + 4$

(c) (i)  $d = \sqrt{(8+5t)^2 + (10-6t)^2}$   
 $= \sqrt{64 + 80t + 25t^2 + 100 - 120t + 36t^2}$   
 $P = \sqrt{61t^2 - 40t + 164}$   
 (ii)  $P' = \frac{1}{2}(61t^2 - 40t + 164)^{-\frac{1}{2}} \times (122t - 40)$   
 $0 = \frac{122t - 40}{2(61t^2 - 40t + 164)^{\frac{1}{2}}}$   
 $0 = 122t - 40$   
 $\therefore t = 0.327 \dots$   
 $\approx 0.33$  hours

showing min.  $\frac{1}{2}$  (0.33) (0.33) (0.4)

(i) Distance Apart  $= \sqrt{61(0.33)^2 - 40(0.33) + 164}$   
 $\approx 12.5$  km.  
 Question 6 (12)

(a)  $y = x(x-3)^3$   
 (i)  $y' = (x-3)^3 + x \cdot 3(x-3)^2$   
 $0 = (x-3)^2 [x-3+3x]$   
 $x = 3$  or  $x = \frac{3}{2}$  (60%)  
 $y = 0$  or  $y = -\frac{27}{8} = -8.54$   
 $y'' = 2(x-3)(4x-3) + (x-3)^2 \cdot 4$   
 $y''(3) = 0$  (3:0) horizontal pt. of inf.  
 $y''(\frac{3}{2}) = \frac{81}{4} > 0 \therefore (\frac{3}{2}, -8.54)$  Min. turning

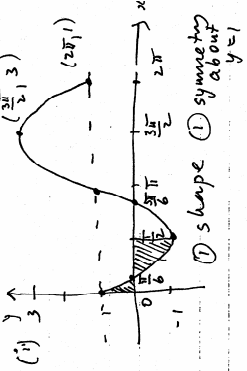
(ii)  $y'' = 2(x-3)[6x-9] = 0$   
 $x = 3$  or  $x = \frac{3}{2}$   
 $y = 0$  or  $y = -\frac{81}{16}$   
 (3:0) horiz. pt. of inf.  
 $x = \frac{3}{2}$  or  $y = -\frac{81}{16}$  Concavity changes  
 $\therefore (\frac{3}{2}, -\frac{81}{16})$  pt. of inf.  


Question 6 - cont.

(b)  $6x^2 - 2x + 5 = 0$   
 (i)  $\alpha + \beta = -\frac{b}{a} = \frac{1}{6}$   
 (ii)  $\alpha - \beta = \frac{c}{a} = \frac{5}{6}$   
 (iii)  $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$   
 $= (\frac{1}{6})^2 - 2 \times \frac{5}{6} = -\frac{59}{36}$

(c)  $\log_3 32 = x \cdot \log_3 2$   
 $\frac{\log_3 32}{\log_3 2} = \log_3 2^x$   
 $\frac{\log_3 32}{3} = \log_3 2^x$   
 $\frac{1}{3} \log_3 32 = \log_3 2^x$   
 $\log_3 32^{\frac{1}{3}} = \log_3 2^x$   
 $32^{\frac{1}{3}} = 2^x$   
 $(2^5)^{\frac{1}{3}} = 2^x$   
 $\frac{5}{3} = x$

Question 7 (12)

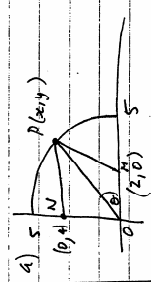


(i) cuts x-axis:  $y = 0$   
 $0 = 1 - 2\sin x$   
 $2\sin x = 1 \therefore x = \frac{\pi}{6}, \frac{5\pi}{6}$

(ii) Area  $= \int_{\frac{\pi}{6}}^{\frac{5\pi}{6}} (1 - 2\sin x) dx$   
 $= [x + 2\cos x]_{\frac{\pi}{6}}^{\frac{5\pi}{6}}$   
 $= \frac{\pi}{6} + 2\cos \frac{\pi}{6} - 0 - 2\cos 0 + \frac{\pi}{6} + 2\cos \frac{\pi}{6} - \frac{\pi}{6}$   
 $= \frac{\pi}{6} + 2 \times \frac{\sqrt{3}}{2} - 2 + \frac{\pi}{6} + 2 \times \frac{\sqrt{3}}{2} - \frac{\pi}{6}$   
 $= 0.2556 + 9 - 0.68485$   
 $= 0.94$   
 (The correct answer includes the knowledge of the abs. value)

(b) (i)  $\cos(2.08) = \frac{5^2 + 6^2 - r^2}{2 \times 5 \times 6}$   
 $\cos(2.08) = 1.287$  radians  
 (ii)  $A = \frac{1}{2} r^2 \theta - \frac{1}{2} r^2 \sin \theta$   
 $= \frac{1}{2} \times 5^2 \times 2.08 - \frac{1}{2} \times 5^2 \sin 2.08 = 4.0875$

Question 10 (12)



1)  $A_{ODHP} = \frac{1}{2} OH \times OP \times \sin \theta$   
 $= \frac{1}{2} \times 2 \times 5 \times \sin \theta$   
 $= 5 \sin \theta$  ①

$A_{ODPU} = \frac{1}{2} ON \times OP \times \sin(90^\circ - \theta)$   
 $= \frac{1}{2} \times 4 \times 5 \times \cos \theta$   
 $= 10 \cos \theta$

$\therefore A = 5 \sin \theta + 10 \cos \theta$

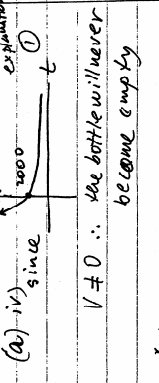
ii)  $A' = 5 \cos \theta - 10 \sin \theta$   
 $0 = 5 \cos \theta - 10 \sin \theta$   
 $10 \sin \theta = 5 \cos \theta$   
 $\tan \theta = \frac{1}{2}$

showing Max:  $\tan \theta = \frac{1}{2} \therefore \theta = 26.56^\circ$

$A'' = -5 \sin \theta - 10 \cos \theta$  ①  
 $A''(\theta = 26.56^\circ) = -11.18 < 0 \therefore$  Max.

iii) since  $\tan \theta = \frac{1}{2} = \frac{y}{x}$   
 $\therefore \frac{1}{2} = \frac{y}{x}$   
 $2y = x + y$   
 $x = \sqrt{20} = 2\sqrt{5}$   
 $y = \frac{\sqrt{20}}{2} = \sqrt{5}$  ①

Q.9 cont.



(a)  $\therefore$  she bottle will never become empty

$V \neq 0$

$\therefore \frac{1}{2} a = 25$   
 $\frac{1}{2} a = 25$   
 $a = 50$

$\therefore S_n = 117 = \frac{n}{2} (2 \times 25 - (n-1) \times 5)$   
 or  $117 = 25n - \frac{5n(n-1)}{2}$   
 $234 = 50n - 5n^2 + 5n$   
 $5n^2 - 55n + 234 = 0$

ii) box only ①

(c)  $1.25 = 1.2 + \frac{5}{100} + \dots$  ①  
 or  $1 + \frac{2}{10} + \frac{5}{100} + \dots$

$\therefore 1.25 = 1.2 + \frac{a}{1-r}$   
 $0.05 = \frac{a}{1-r}$   
 $0.05(1-r) = a$   
 $0.05 - 0.05r = a$   
 $0.05 - 0.05 \times \frac{5}{100} = a$   
 $0.05 - 0.0025 = a$   
 $a = 0.0475$

(d)  $V = \int_0^3 \pi (e^{2x} - 1)^2 dx$   
 $= \pi \int_0^3 (e^{4x} - 2e^{2x} + 1) dx$  ①  
 $= \pi \left[ \frac{1}{4} e^{4x} - e^{2x} + x \right]_0^3$  ①  
 $= \pi \times 165.285 = 519.26$  ①

Q.7 cont.

$\therefore d = \left[ 10t^2 - \frac{5}{3}t^3 \right]_0^4 + \left[ 10t^2 - \frac{5}{3}t^3 \right]_4^5$   
 $= \frac{160}{3} + \left[ 10 \times 25 - \frac{5}{3} \times 125 \right] - \left[ 10 \times 16 - \frac{5}{3} \times 64 \right]$   
 $d = \frac{320}{3} = 106.67 \text{ m}$  ①

(b)  $\angle C$  in common  
 $\angle ABC = \angle EDC = 90^\circ$  (given) ①  
 $\therefore \Delta ABC \sim \Delta CDE$  (matching  $\angle$ s =  $\angle$ )

(ii)  $\frac{EC}{AC} = \frac{CD}{BC}$  (matching sides in the same ratio) ①

$\therefore BC \times CE = AC \times CD$

(iii) using (i) ②  
 $BC \times CE = AC \times CD$   
 $(BE + EC) \times CE = (AD + DC) \times CD$   
 $BE \cdot EC + EC^2 = AD \cdot DC + DC^2$

By transposition  
 $BE \cdot EC - DC^2 = AD \cdot DC - BE \cdot EC$   
 $DE^2 = AD \cdot DC - BE \cdot EC$   
 $\therefore$  slow

Question 9 ⑫

(a)  $V = 2000e^{-0.005t}$

i)  $t = 0 \therefore V = 2000 \text{ mL}$  ①  
 ii)  $V = 2000e^{-0.005 \times 30} = 1721.41$   
 $\therefore$  evaporated  $2000 - 1721.41 = 278.58 \text{ mL}$  ①

iii)  $1000 = 2000e^{-0.005t}$   
 $\ln \frac{1}{2} = -0.005t$   
 $t = 138.629 \text{ hours}$  ①

Question 8 (12)

a)  $V = 5t(4-t) = 20t - 5t^2$   
 $t = 0 \quad V = 0 \quad x = 0$

i)  $a = \frac{dV}{dt} = 20 - 10t$  ①  
 $a(t=4) = 20 - 10 \text{ m/s}^2$  ①

ii)  $x = \int v dt = \int 20t - 5t^2 dt$   
 $x = 10t^2 - \frac{5}{3}t^3 + c$  ①  
 $0 = 0 - 0 + c \therefore c = 0$  ①  
 $\therefore x = 10t^2 - \frac{5}{3}t^3$

iii)  $V = 20t - 5t^2 = 5t(4-t)$

$d = \int_0^4 (20t - 5t^2) dt + \int_4^6 (20t - 5t^2) dt$  ①

$d = \left[ 10t^2 - \frac{5}{3}t^3 \right]_0^4 + \left[ 10t^2 - \frac{5}{3}t^3 \right]_4^6$   
 $= \left[ 10 \times 16 - \frac{5}{3} \times 64 \right] - \left[ 10 \times 16 - \frac{5}{3} \times 64 \right] + \left[ 10 \times 36 - \frac{5}{3} \times 216 \right] - \left[ 10 \times 16 - \frac{5}{3} \times 64 \right]$   
 $= 0 + \left[ 360 - 360 \right] - \left[ 160 - 106.67 \right]$   
 $= 0 - 53.33 = -53.33$

8.10 cont.

$$b) i) A_1 = 450000 \times \left(1 + \frac{1.25}{100}\right) - 6000 \quad \textcircled{1}$$
$$= 450000 \times 1.0125 - 6000$$

$$(ii) A_2 = A_1 \times 1.0125 - 6000$$
$$= 450000 \times 1.0125^2 - 6000 \times 1.0125 - 6000$$

$$\dots A_n = 450000 \times 1.0125^n - 6000 \times 1.0125^{n-1} - \dots - 6000 \quad \textcircled{1}$$

OR  $A_n = 450000 \times 1.0125^n - 6000 \left[1 + 1.0125 + \dots + 1.0125^{n-1}\right] \quad \textcircled{1}$

$$iii) D = 450000 \times 1.0125^n - 6000 \times \frac{1.0125^n - 1}{1.0125 - 1} \quad \textcircled{1}$$

$$0 = 450000 \times 1.0125^n - 480000 \left(\frac{1.0125^n - 1}{1.0125 - 1}\right)$$

$$0 = 450000 \times 1.0125^n - 480000 \times 1.0125^n + 480000$$

$$\therefore 30000 \times 1.0125^n = 480000$$

$$1.0125^n = 16$$

$$n = \frac{\ln 16}{\ln 1.0125}$$

$$\textcircled{1} \quad n = 223.19 \text{ months}$$

$$= 18.59 \text{ yrs (18 yrs 7.2 months)}$$

(iv) Try  $r = 16\%$ .  $\therefore r = \frac{16}{100}$

$$\therefore 450000 \times (1.013)^{360} = 6000 \left(\frac{(1.013)^{360} - 1}{1.013 - 1}\right)$$

$$\therefore 450000 \times (1.013)^{360} = 6000 \times (8753. \dots)$$

$$\frac{450000 \times (1.013)^{360}}{8753. \dots} = 6052 \approx 6000 \quad \textcircled{1}$$